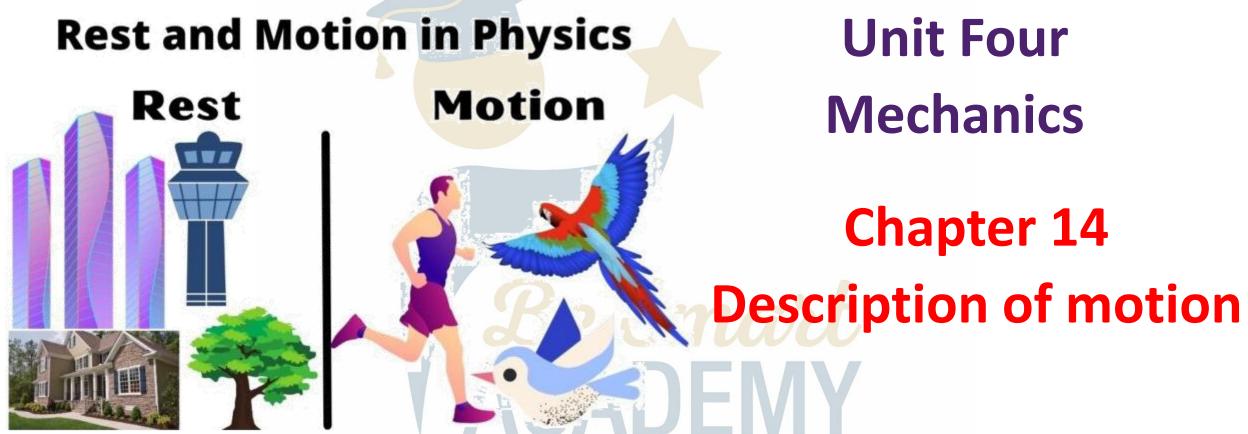
### **Physics – Grade 10**





Prepared & Presented by: Mr. Mohamad Seif







1 Introduction about mechanics

2 Definition of motion

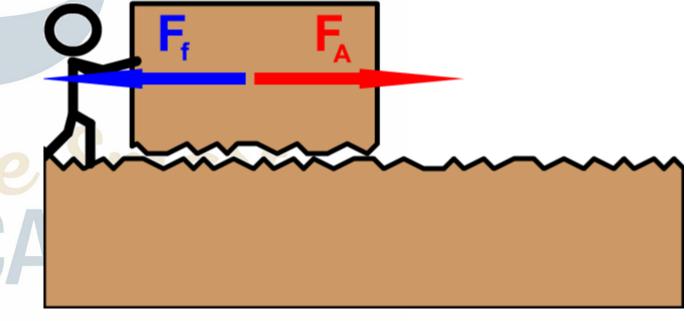
2 Space and time frames of reference:

#### **Definition of mechanics**

# Be Smart ACADEMY

#### What is "Mechanics"?

Mechanics is a branch of physics that studies the state (motion or rest) of an object (or system) and taking into consideration its causes.



#### **Definition of mechanics**



#### **Kinematics**

Concerned with Concerned with Concerned with the motion without reference to the cause of motion

#### **Statics**

**Mechanics** 

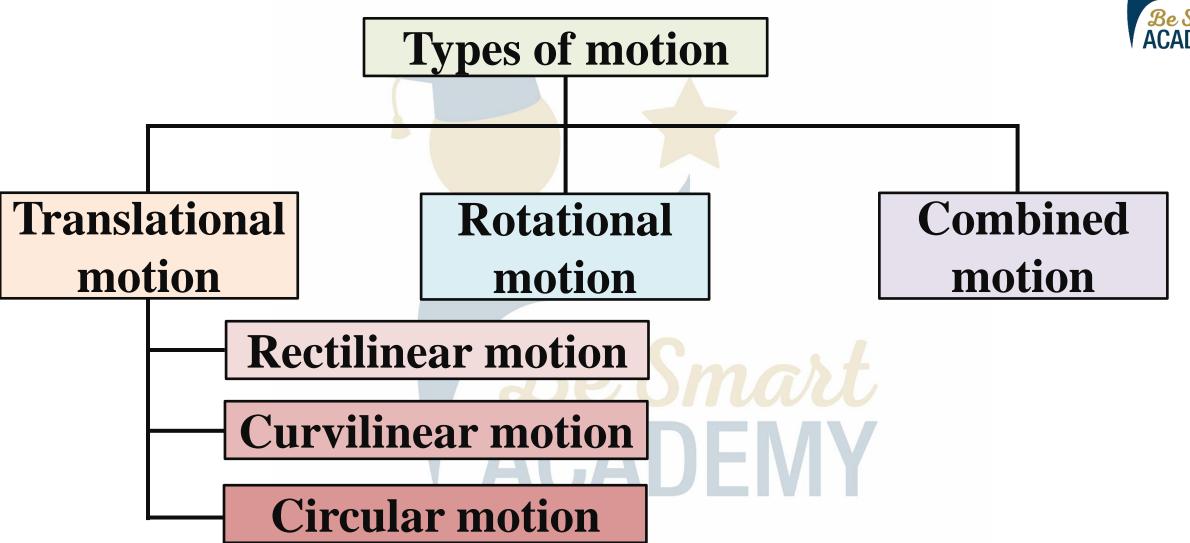
system during (force, energy...) static equilibrium

#### **Dynamics**

the description of analysis of loads study of motion (forces, torque...) with reference to acting on a the cause of motion

#### **Definition of mechanics**





#### **Definition of motion**

# Be Smart ACADEMY

#### **Rest & motion:**

The terms "at rest" or "in motion" are relative and depend on the chosen reference.

The same object may be at rest with respect to a certain observer and in motion with respect to another.



B is at rest relative to A
C is in motion relative to A
C is in motion relative to B

#### **Definition of motion**



Motion is defined as a change of position of a body relative to a reference point.

Trajectory of a moving object:

The trajectory of motion is the path described by this object during its motion.

The trajectory of rectilinear motion is straight line.

#### Space and time frames of reference:



The space frame of reference is used to determine the position and the distance covered by a moving object in this frame.

The origin of the reference is the point of observation of the motion.

The space reference system of a particle moving on a rectilinear trajectory is denoted by  $(0, \vec{t})$ .



#### Space and time frames of reference:



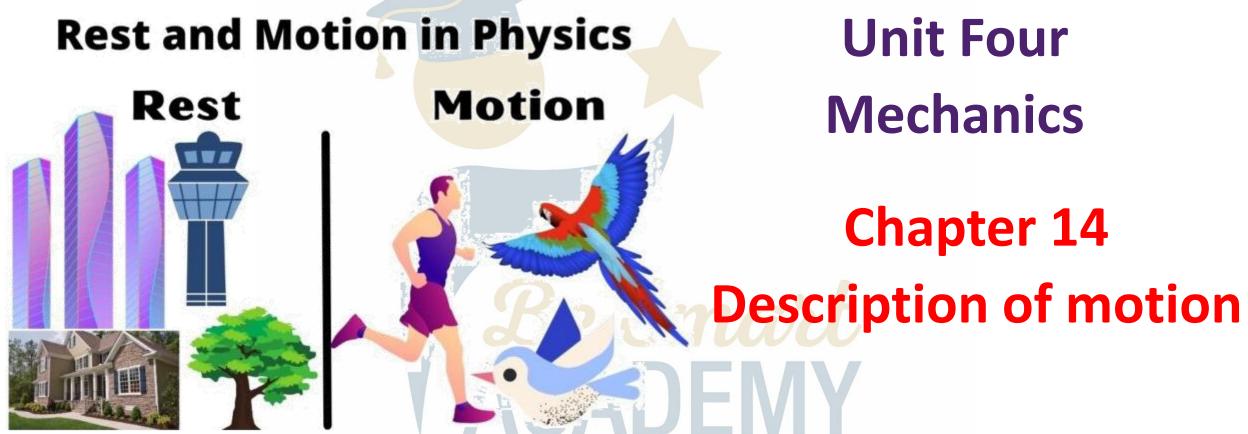
- The choice of a time reference is used to know the instant of an event and to determine the duration of motion.
- The time  $t_0 = 0s$  is taken to be the origin of time of most events, where it indicates the instant of starting the studying of the motion and not necessarily the instant of starting the motion.





### Physics – Grade 10





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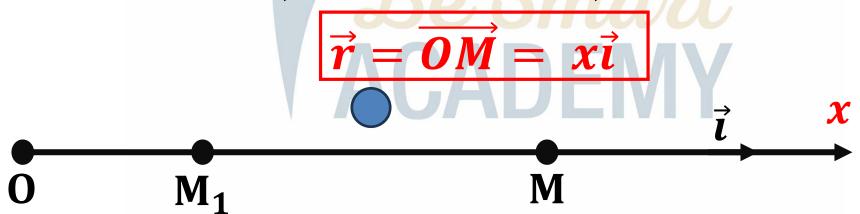




**Distance and Displacement** 

ACADEMY

- Be Smart ACADEMY
- The rectilinear motion of a body M is studied with respect to the frame  $(0, \vec{i})$ , of origin O.
- The position of the body at the origin of time  $t_0 = 0$ , is at O such that  $x_0 = 0$  and its position at an instant t, is x = OM.
- The position vector, at an instant t, is:





### Characteristic of the position vector $\overrightarrow{OM_1}$ :

- Origin: C
- Line of action: The horizontal line holding O and  $M_1$



- Direction: The motion is from O to  $M_1$ : To right
- Magnitude:  $|\vec{r}_1| = |\overrightarrow{OM_1}|$

# Be Smart ACADEMY

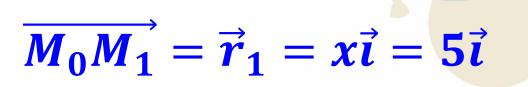
#### **Application 1:**

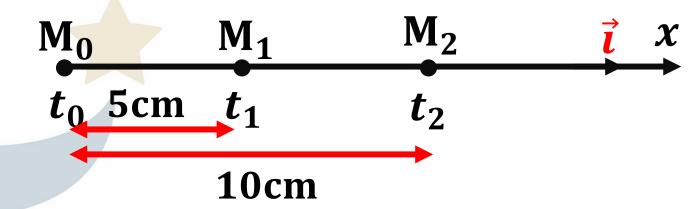
- Consider a particle moving along the x-axis and starting from  $M_0$  at  $t_0 = 0$ .
- The particle passes through  $M_1$  then  $M_2$  as shown in the figure.
- 1.What is the nature of motion? Justify.  $t_0$   $t_0$   $t_1$   $t_2$   $t_2$   $t_3$   $t_4$   $t_5$   $t_6$   $t_6$   $t_7$   $t_8$   $t_8$   $t_9$   $t_9$

Since the particle moves on a straight line, the motion is rectilinear



### 2. Determine the position vector $\overline{M_0M_1}$ .





3. Determine the position vector  $\overline{M_0M_2}$ .

$$\overrightarrow{M_0M_2} = \overrightarrow{r}_2 = x\overrightarrow{i} = 10\overrightarrow{i}$$



 $M_2$ 

 $M_1$ 

10cm

5. Determine the characteristics of the position vector  $\overline{M_0M_1}$ .

- Origin:  $M_0$
- Line of action:

The horizontal line holding  $M_0$  and  $M_1$ 

• Direction: To the right

• Magnitude:

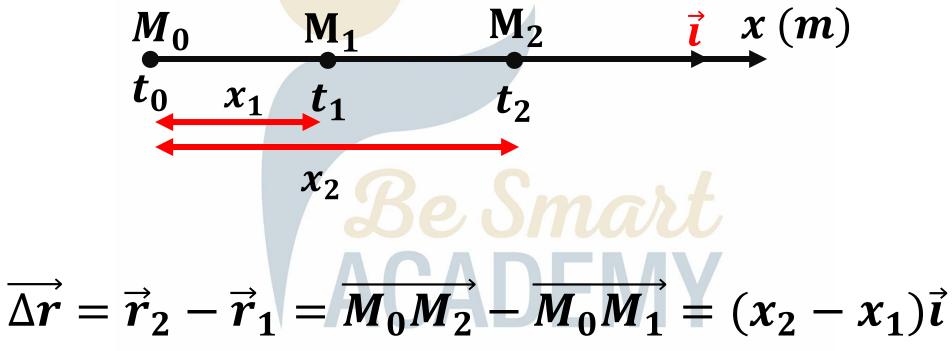
$$|\vec{r}_1| = |\overrightarrow{M_0 M_1}| = 5cm$$

 $t_0$  5cm

# Be Smart ACADEMY

#### The displacement:

The displacement is the change in position vector between two points.

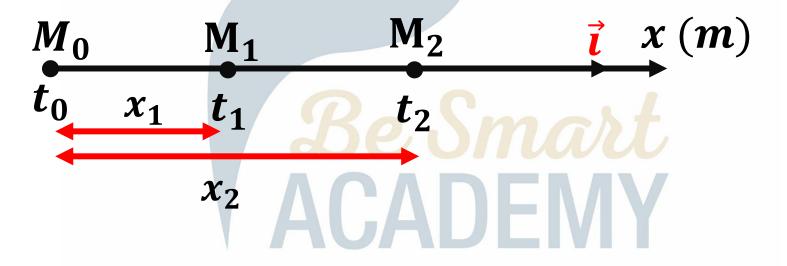


# Be Smart ACADEMY

#### **Distance:**

The actual distance covered by a moving particle in an interval of time.

The distance is a scalar quantity, and its SI unit is meter [m].



$$|\Delta x| = |\Delta \overrightarrow{r}| = |\overrightarrow{M_0 M_2} - \overrightarrow{M_0 M_1}| = |x_2 - x_1|$$

#### **Application 2:**

1.Determine the displacement vector.

$$\overrightarrow{\Delta r} = \overrightarrow{r}_2 - \overrightarrow{r}_1 = \overrightarrow{M_0 M_2} - \overrightarrow{M_0 M_1} \qquad x_1 = 1.3m$$

$$\overrightarrow{\Delta r} = (x_2 - x_1)\overrightarrow{i} \qquad x_2 = 2.5m$$

$$\overrightarrow{\Delta r} = (2.5 - 1.3)\overrightarrow{A}CADEMY$$

$$\overrightarrow{\Delta r} = \mathbf{1.2}\overrightarrow{i}$$





$$\overrightarrow{\Delta r} = \mathbf{1.2}\overrightarrow{i}$$

2.Determine the distance covered during the motion of the particle M between the two instants.

$$|\Delta x| = |\Delta \vec{r}| = |M_0 M_2 - M_0 M_1|$$

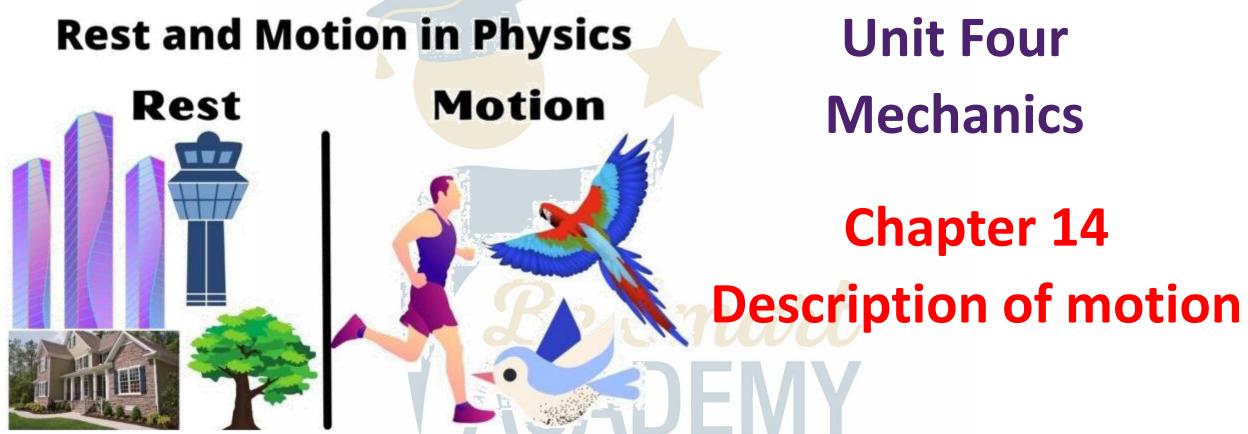
$$= |x_2 - x_1|$$

$$|\Delta x| = |\Delta \vec{r}| = 1.2m \text{ GADE}$$



## Physics – Grade 10





Prepared & Presented by: Mr. Mohamad Seif







1 To calculate average & instantaneous speed

2 To determine the average & instantaneous velocity vector

Be Smart ACADEMY

To study the motion of a moving particle M, the positions of the particle designated by  $M_0 \dots M_5$  are taken over regular time intervals  $\tau$ .

$M_0$	$M_1$	M <sub>2</sub>	$M_3$	$M_4$	$M_5 \vec{l} x$
	+	to	t -	+	<i>t</i> _
$t_0$	<i>L</i> <sub>1</sub>	$\iota_2$	<i>L</i> 3	L <sub>4</sub>	$\iota_5$

#### We must distinguish between the following:

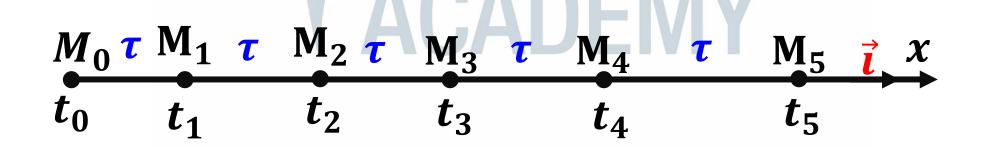
- 1. The average speed.
- 2.Instantaneous speed. A GALE | |
- 3. The average velocity vector.
- 4. The instantaneous velocity vector

## Be Smart ACADEMY

#### Average speed (V<sub>av</sub>):

The average speed (m/s) between two points is the ratio of the total distance traveled to the total duration needed to travel this distance.  $V_{av} = \frac{\text{distance traveled}}{\text{needed time}} = \frac{d}{\Delta t}$ 

Consider a puck moving on an air table, with a time interval between two consecutive points is  $\tau$ 





# $M_2 \& M_4$ is:

$$V_{2,4} = \frac{M_2 M_4}{t_4 - t_2} = \frac{M_2 M_4}{4\tau - 2\tau}$$

The average speed between The average speed between  $M_1 \& M_5$  is:

$$V_{1,5} = \frac{M_1 M_5}{t_5 - t_1} = \frac{M_1 M_5}{5\tau - \tau}$$

$$V_{2,4} = \frac{M_2 M_4}{2\tau}$$
 ACADE $V_{1,5} = \frac{M_1 M_5}{4\tau}$ 

# Be Smart ACADEMY

#### Instantaneous speed (V):

The average speed is not accurate to describe the motion. The Instantaneous speed (V) at instant t is the speed of the moving body at specific time (t).

$$V_{4} = \frac{M_{3}M_{5}}{t_{5} - t_{3}} = \frac{M_{3}M_{5}}{2\tau} \quad ACADE \quad V_{2} = \frac{M_{1}M_{3}}{t_{3} - t_{1}} = \frac{M_{1}M_{3}}{2\tau}$$

$$V_3 = \frac{M_2 M_4}{t_4 - t_2} = \frac{M_2 M_4}{2\tau}$$

#### **Application 3:**



- A puck moves without initial speed on an air table. The time interval between two consecutive points is  $\tau = 60$ ms.
- 1.Determine the average speed of the puck between  $V_{1,2}$ ,  $V_{2,5}$ , and  $V_{1,5}$ .
- 2. Determine the instantaneous speeds  $V_3$ , &  $V_4$  of the puck at the instants  $t_3$ , & at  $t_4$ .

$M_0$ $M_1$	M <sub>2</sub>	$M_3$	M <sub>4</sub>	M <sub>5</sub>
$M_0M_1$	$M_1M_2$	$M_2M_3$	$M_3M_4$	$M_4M_5$
0.5cm	1.5cm	2.5cm	3.5cm	4.5cm



1.Determine the average speed of the puck between

 $V_{1,2}, V_{2,5}$ , and  $V_{1,5}$ .

$M_0  au M_1$	$\tau$ $M_2$ $\tau$	M <sub>3</sub> τ	<b>M</b> <sub>4</sub> <b>T</b>	M <sub>5</sub>
$M_0M_1$	$M_1M_2$	$M_2M_3$	$M_3M_4$	$M_4M_5$
0.5cm	1.5cm	2.5cm	3.5cm	4.5cm

$$V_{1,2} = \frac{M_1 M_2}{t_2 - t_1} = \frac{M_1 M_2}{\tau}$$
  $V_{1,2} = \frac{(1.5 \times 10^{-2})m}{(60 \times 10^{-3})s}$ 

$$V_{1,2} = 0.25m/s$$

$$M_0$$
  $\tau$   $M_1$   $\tau$   $M_2$   $\tau$   $M_3$   $\tau$   $M_4$   $\tau$   $M_5$ 

$M_0M_1$	$M_1M_2$	$M_2M_3$	$M_3M_4$	$M_4M_5$
0.5cm	1.5cm	2.5cm	3.5cm	4.5cm

$$V_{2,5} = \frac{M_2 M_5}{t_5 - t_2}$$



$$V_{2,5} = \frac{M_2 M_5}{3\tau}$$

$$V_{2,5} = \frac{(2.5 + 3.5 + 4.5) \times 10^{-2}}{(3 \times 60 \times 10^{-3})s}$$



$$V_{2,5} = \frac{10.5 \times 10^{-2}}{(180 \times 10^{-3})}$$

$$V_{2.5} = 0.583m/s$$



$M_0$ $\tau$	$M_1$	τ	$M_2$	τ	$M_3$	τ	$M_4$	τ	$M_5$

$M_0M_1$	$M_1M_2$	$M_2M_3$	$M_3M_4$	$M_4M_5$
0.5cm	1.5cm	2.5cm	3.5cm	4.5cm

$$V_{1,5} = \frac{M_1 M_5}{t_5 - t_1}$$



$$V_{1,5} = \frac{M_1 M_5}{4\tau}$$

$$V_{1,5} = \frac{(1.5 + 2.5 + 3.5 + 4.5) \times 10^{-2}m}{4 \times 60 \times 10^{-3}s}$$



$$V_{1,5} = \frac{12 \times 10^{-2} m}{240 \times 10^{-3} s}$$

$$V_{1.5} = 0.5 m/s$$



2. Determine the instantaneous speeds  $V_3$  &  $V_4$  of the

puck at the instants  $t_2$ , & at  $t_3$ .

τ	M <sub>1</sub>	τ	M <sub>2</sub>	τ	M <sub>3</sub>	τ	M <sub>4</sub>	τ	M <sub>5</sub>	
	$M_0$ M	<b>1</b> <sub>1</sub>	N	$M_1M_2$		$M_2M$	13	$M_3M_4$	<sub>L</sub> M	$_4M_5$
	0.5c	m		L.5cm		2.5c	m	3.5cm	4.	5cm

$$V_3 = \frac{M_2 M_4}{t_4 - t_2}$$

$$V_3 = \frac{(1.5 + 2.5) \times 10^{-2} m}{(2 \times 60 \times 10^{-3})s}$$



 $V_3 = 0.333m/s$ 

 $M_0$   $\tau$   $M_1$   $\tau$   $M_2$   $\tau$   $M_3$   $\tau$   $M_4$   $\tau$   $M_4$ 

$M_0M_1$	$M_1M_2$	$M_2M_3$	$M_3M_4$	$M_4M_5$
0.5cm	1.5cm	2.5cm	3.5cm	4.5cm

$$V_4 = \frac{M_3 M_5}{t_5 - t_3}$$



$$V_4 = \frac{M_3 M_5}{2\tau}$$

 $V_4 = \frac{(2.5 + 3.5) \times 10^{-2} m}{(2 \times 60 \times 10^{-3})s}$ 

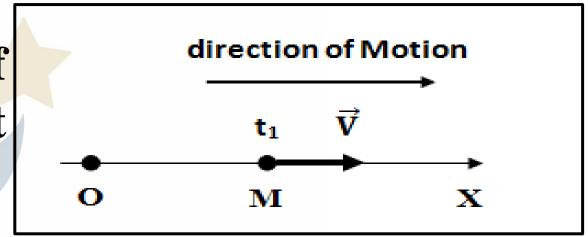


$$V_4 = 0.5 m/s$$

## Be Smart ACADEMY

### The velocity vector $(\overrightarrow{V})$ :

The velocity vector is the rate of change of position with respect to time.



Velocity (m/s) represents how fast an object moves with direction.

The velocity is a vector whose magnitude is called speed, and its sign depends on the direction of motion  $\vec{V} = V \cdot \vec{\iota}$ .

# Be Smart ACADEMY

## The average velocity vector $(\vec{V}_{av})$ :

The average velocity measures the variation of the position vector of a moving particle during an in interval of time. The average velocity is represented by the vector:

$$\vec{V}_{av} = \frac{\Delta \vec{r}}{\Delta t} = \frac{(x_2 - x_1) \cdot \vec{t}}{t_2 - t_1}$$

# Be Smart ACADEMY

## The instantaneous velocity vector $(\vec{V}_{av})$ :

The instantaneous velocity measures the variation of the position vector of a moving particle w. r. t time at a given instant.

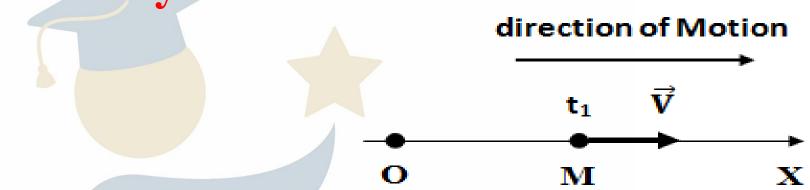
The instantaneous velocity is represented by the vector:

$$\overrightarrow{V} = V. \overrightarrow{i}$$

Where V is the instantaneous speed.

**Characteristics of velocity vector:** 





Origin	point M
Line of action	horizontal and rectilinear.
<b>Direction:</b>	To the right
Magnitude:	Is the speed at point M, to be calculated



Application 4: A puck moves without initial speed on an air table as shown.

- The time interval between two consecutive points is  $\tau = 60ms$ .
- 1. Calculate the instantaneous speed at  $M_3$ .
- 2. Determine the characteristics of the velocity vector at  $t_3$ .

$\mathbf{M_0}$	$\mathbf{M_1}$	$M_2$	$M_3$	$\mathbf{M_4}$	$\mathbf{M_5}$
				100 T.	

$M_0M_1$	$M_1M_2$	$M_2M_3$	$M_3M_4$	$M_4M_5$
0.5cm	1.5cm	2.5cm	3.5cm	4.5cm

$$\tau = 60ms = (60 \div 1000) = 0.06 s$$

1. Calculate the instantaneous speed at  $M_3$ .

<b>M</b> <sub>0</sub>	M <sub>1</sub>	M <sub>2</sub>	$M_3$	14	M <sub>5</sub>
N	$M_0M_1$	$M_1M_2$	$M_2M_3$	$M_3M_4$	$M_4M_5$
C	).5cm	1.5cm	2.5cm	3.5cm	4.5cm

$$V_3 = \frac{M_2 M_4}{t_4 - t_2}$$
  $\searrow$   $V_3 = \frac{M_2 M_4}{2\tau}$   $\searrow$   $V_3 = \frac{(4 \times 10^{-2})m}{(2 \times 0.06)}$ 

$$V_3 = 0.333m/s$$

$$\tau = 0.06 s$$
;  $V_3 = 0.375 m/s$ 

2. Determine the characteristics of the velocity vector at  $t_3$ .

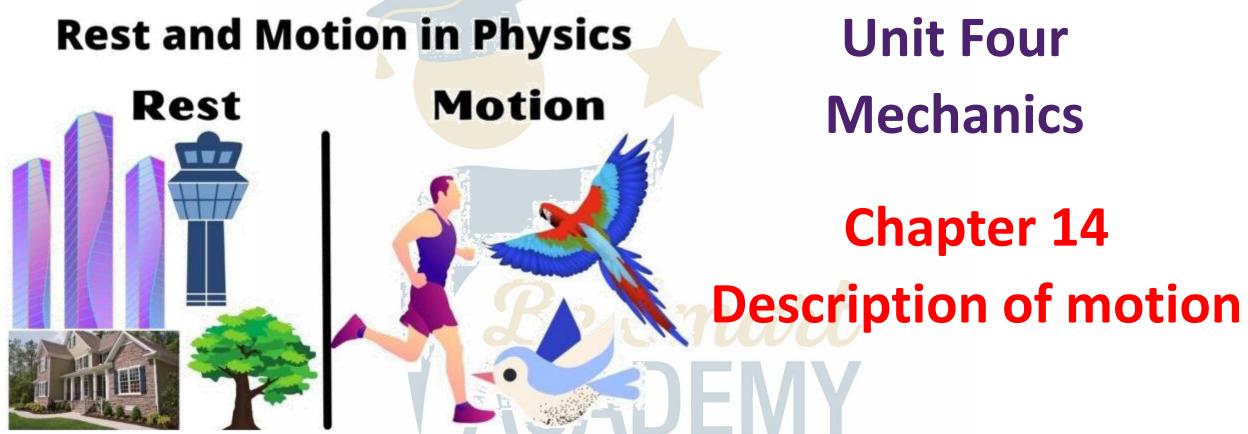


Origin	point M <sub>3</sub>
Line of action	horizontal and rectilinear.
<b>Direction:</b>	To right
Magnitude:	$V_3 = 0.333m/s$



## Physics – Grade 10





Prepared & Presented by: Mr. Mohamad Seif







1 To calculate average & instantaneous acceleration

2 To determine the characteristics of acceleration vector.

# Be Smart ACADEMY

## Acceleration (a):

Acceleration is a quantity used to describe the variations of the speed of a moving particle with respect to time.

$$a = \frac{change of velocity}{change of time} = \frac{\Delta V}{\Delta t}$$

- The acceleration expressed in is  $m/s^2$
- 1.Average acceleration. A GADEMY
- 2.Instantaneous acceleration.
- 3. Acceleration vector (average and Instantaneous).



## Average acceleration:

Average acceleration is the variation of the speed of a moving particle between two instants with respect to time.

$\mathbf{M_0}$	$\mathbf{M_1}$	$M_2$	$M_3$	$\mathbf{M_4}$	$\mathbf{M_5}$

$$\mathbf{a}_{\mathrm{av}} = \frac{\Delta V}{\Delta t} = \frac{V_f - V_i}{t_f - t_i}$$



$$\mathbf{a}_{\mathrm{av}} = \frac{\Delta V}{\Delta t} = \frac{V_f - V_i}{t_f - t_i}$$



The average acceleration The average acceleration between M<sub>1</sub>& M<sub>4</sub> is:

between M<sub>1</sub>& M<sub>4</sub> is:

$$a_{1,4} = \frac{V_4 - V_1}{t_4 - t_1}$$
 AGAIL  $a_{2,5} = \frac{V_5 - V_2}{t_5 - t_2}$ 



## Average acceleration vector $(\vec{V}_{av})$ :

Average acceleration vector is a vector represent the variation of the speed of a moving particle between two instants with respect to time.

$$\vec{a}_{av} = \frac{\Delta \vec{V}}{\Delta t} = \frac{\vec{V}_f - \vec{V}_i}{t_f - t_i}$$



Application 5: The figure below shows the positions of a puck during an intervals of time  $\tau = 60ms$ .

$$G_0 \stackrel{\leftarrow}{\downarrow} G_{12.7cm} G_2$$
 3.9cm  $G_3$  5.1cm  $G_4$  6.3cm  $G_5$  7.5cm  $G_6$   $x$ 

- At  $t_0 = 0s$ , the puck starts from  $G_0$  and is initially at rest.
- 1. Calculate the instantaneous speeds  $V_1$ ;  $V_3$  and  $V_5$ .
- 2. Calculate the average acceleration between  $G_1\& G_3$  and between  $G_3\& G_5$ .
- 3. Deduce the average acceleration vector between  $G_1\&G_3$ .

$$\tau = 60ms = (60 \div 1000) = 0.06 s; V_0 = 0$$

$$G_0 = G_{12.7cm} G_2 = 3.9cm = G_3 = 5.1cm = G_4 = 6.3cm = G_5 = 7.5cm = G_6 = \chi$$

## 1. Calculate the instantaneous speeds $V_1$ ; $V_3$ and $V_5$ .

$$V_{1} = \frac{G_{0}G_{2}}{t_{2} - t_{0}}$$

$$V_{1} = \frac{G_{0}G_{1} + G_{1}G_{2}}{2\tau - 0}$$

$$V_{1} = \frac{G_{0}G_{1} + G_{1}G_{2}}{2\tau - 0}$$

$$V_{1} = \frac{4.2 \times 10^{-2}}{2 \times 0.06}$$

$$V_1 = 0.35 m/s$$



$$\tau = 60ms = (60 \div 1000) = 0.06 s; V_0 = 0$$

$$G_0 \subseteq G_{12.7cm} G_2$$
 3.9cm  $G_3$  5.1cm  $G_4$  6.3cm  $G_5$  7.5cm  $G_6$   $\chi$ 

## 1. Calculate the instantaneous speeds $V_1$ ; $V_3$ and $V_5$ .

$$V_3 = \frac{G_2G_4}{t_4 - t_2} \qquad V_3 = \frac{G_2G_3 + G_3G_4}{4\tau - 2\tau}$$

$$V_3 = \frac{(3.9 + 5.1) \times 10^{-2}}{2\tau} \longrightarrow U_3 = \frac{9 \times 10^{-2}}{2 \times 0.06}$$

$$V_3 = 0.75 m/s$$



$$\tau = 60ms = (60 \div 1000) = 0.06 s; V_0 = 0$$

$$G_0 \stackrel{\mathsf{G}}{=} G_{12.7 \text{cm}} G_2$$
 3.9cm  $G_3$  5.1cm  $G_4$  6.3cm  $G_5$  7.5cm  $G_6$   $\chi$ 

## 1. Calculate the instantaneous speeds $V_1$ ; $V_3$ and $V_5$ .

$$V_{5} = \frac{G_{4}G_{6}}{t_{6} - t_{4}}$$

$$V_{5} = \frac{G_{4}G_{5} + G_{5}G_{6}}{6\tau - 4\tau}$$

$$V_{5} = \frac{(6.3 + 7.5) \times 10^{-2}}{2\tau}$$

$$V_{5} = \frac{13.8 \times 10^{-2}}{2 \times 0.06}$$

$$V_5 = 1.15 m/s$$



$$\tau = 0.06 s$$
;  $V_0 = 0$ ;  $V_1 = 0.35 m/s$ ;  $V_3 = 0.75 m/s$ ;  $V_5 = 1.15 m/s$ 

## 2. Calculate the average acceleration between $G_1 \& G_3$ and between G<sub>3</sub> & G<sub>5</sub>

$$a_{1,3} = \frac{V_3 - V_1}{t_3 - t_1} \implies$$

$$a_{1,3} = \frac{V_3 - V_1}{t_3 - t_1} \implies a_{1,3} = \frac{0.75 - 0.35}{2\tau} \implies a_{1,3} = \frac{0.4}{2 \times 0.06}$$

$$a_{1,3} = \frac{3.11}{2 \times 0.06}$$

$$a_{1,3} = 3.33m/s^2$$

$$a_{3,5} = \frac{V_5 - V_3}{t_5 - t_2}$$

$$a_3 = \frac{1.15 - 0.75}{1.15 - 0.75}$$



$$a_{3,5} = \frac{3.1}{2 \times 0.06}$$

$$a_{3.5} = 3.33 m/s^2$$



$$\tau = 0.06 \text{ s}; V_0 = 0; V_1 = 0.35 \text{m/s}; V_3 = 0.75 \text{m/s}; V_5 = 1.15 \text{m/s}$$

## 3. Represent the average acceleration vector between $G_1 \& G_3$ .

$$G_0 \stackrel{\xi_5}{=} G_{1_{2.7 \text{cm}}} G_2$$
 3.9cm  $G_3$  5.1cm  $G_4$  6.3cm  $G_5$  7.5cm  $G_6$   $\chi$ 

$$\overrightarrow{a}_{1,3} = a_{1,3} \cdot \overrightarrow{\iota}$$



$$\vec{a}_{1,3} = 3.33.\vec{i} \ (m/s^2)$$

$$1cm \rightarrow 1.65m/s^2$$

$$x = ?? \rightarrow 3.33m/s^2$$

$$x = ?? \rightarrow 3.33m/s^2$$

$$x = \frac{1cm \times 3.33}{1.65} \approx 2cm$$



## **Instantaneous acceleration:**

The average acceleration does not give an accurate value to describe the motion of a mobile.

Instantaneous acceleration is the exact description of the variation of the speed at a given instant.





$$M_0$$
  $M_1$   $M_2$   $M_3$   $M_4$   $M_5$ 

# The instantaneous acceleration at $M_2$ : The instantaneous acceleration at $M_4$



$$a_2 = \frac{V_3 - V_1}{t_3 - t_1} \qquad a_4 = \frac{V_5 - V_3}{t_5 - t_3}$$

# Be Smart ACADEMY

## **Instantaneous acceleration vector:**

The instantaneous acceleration vector describes the variation of the speed at a given instant in a given direction.

$$\vec{V}_2 = V_2 \cdot \vec{\iota}$$



Application 6: The figure below shows the positions of a puck during an intervals of time  $\tau = 40ms$ . At  $t_0 = 0s$ .

$$M_{0 1cm}$$
  $M_{11.7cm}M_{2}$  2.4cm  $M_{3}$  3.1cm  $M_{4}$  3.8cm  $M_{5}$   $\chi$ 

- At  $t_0 = 0s$ , the puck starts from from  $M_0$  with  $V_0 = 0.1625$ m/s.
- 1. Calculate the instantaneous speeds  $V_2$ ;  $V_3$  and  $V_4$ .
- 2. Calculate the instantaneous acceleration at  $M_1$  and at  $M_3$ .
- 3. Determine the characteristics of instantaneous acceleration vector at  $M_3$ .



$$\tau = 40ms = (40 \div 1000) = 0.04 s; V_0 = 0.1625 m/s$$

1. Calculate the instantaneous speeds  $V_2$ ;  $V_3$  and  $V_4$ .

$$M_{0 1cm}$$
  $M_{11.7cm}M_{2}$  2.4cm  $M_{3 3.1cm}$   $M_{4 3.8cm}$   $M_{5 \chi}$ 

$$V_2 = \frac{M_1 M_3}{t_3 - t_1} \implies V_2 = \frac{M_1 M_2 + M_2 M_3}{3\tau - \tau} \implies V_2 = \frac{(1.7 + 2.4) \times 10^{-2}}{2\tau}$$

$$V_2 = \frac{4.1 \times 10^{-2}}{2 \times 0.04}$$



AGADEIVIY  $V_2 = 0.5125m/s$ 



$$\tau = 40ms = (40 \div 1000) = 0.04 s; V_0 = 0.1625 m/s$$

1. Calculate the instantaneous speeds  $V_2$ ;  $V_3$  and  $V_4$ .

$$M_{0 1cm}$$
  $M_{11.7cm}M_{2}$  2.4cm  $M_{3 3.1cm}$   $M_{4 3.8cm}$   $M_{5 x}$ 

$$V_3 = \frac{M_2 M_4}{t_4 - t_2} \quad \Longrightarrow \quad V_3 = \frac{M_2 M_3 + M_3 M_4}{4\tau - 2\tau} \quad \Longrightarrow \quad V_3 = \frac{(2.4 + 3.1) \times 10^{-2}}{2\tau}$$

$$V_3 = \frac{5.5 \times 10^{-2}}{2 \times 0.04}$$

$$V_3 = 0.6875 m/s$$



$$\tau = 40ms = (40 \div 1000) = 0.04 s; V_0 = 0.1625 m/s.$$

1. Calculate the instantaneous speeds  $V_2$ ;  $V_3$  and  $V_4$ .

$$M_{0 1cm}$$
  $M_{11.7cm}M_{2}$  2.4cm  $M_{3}$  3.1cm  $M_{4}$  3.8cm  $M_{5}$   $\chi$ 

$$V_4 = \frac{M_3 M_5}{t_5 - t_3} \implies V_4 = \frac{M_3 M_4 + M_4 M_5}{5\tau - 3\tau} \implies V_4 = \frac{(3.1 + 3.8) \times 10^{-2}}{2\tau}$$

$$V_4 = \frac{6.9 \times 10^{-2}}{2 \times 0.04}$$

 $V_4 = 0.8625 m/s$ 



$$\tau = 0.04 s$$
;  $V_0 = 0.1625 m/s$ ;  $V_2 = 0.5125 m/s$ ;  $V_3 = 0.6875 m/s$ ;  $V_4 = 0.8625 m/s$ 

## 2. Calculate the instantaneous acceleration at $M_1$ and at $M_3$ .

$$a_1 = \frac{V_2 - V_0}{t_2 - t_0}$$



$$a_1 = \frac{0.5125 - 0.1625}{2\tau - 0}$$

$$a_1 = \frac{0.35}{2 \times 0.04}$$



$$a_1 = 4.375 m/s^2$$



$$\tau = 0.04 s$$
;  $V_0 = 0$ ;  $V_2 = 0.5125 m/s$ ;  $V_3 = 0.6875 m/s$ ;  $V_4 = 0.8625 m/s$ 

## 2. Calculate the instantaneous acceleration at $M_1$ and at $M_3$ .

$$a_3 = \frac{V_4 - V_2}{\mathsf{t}_4 - \mathsf{t}_2}$$



$$a_3 = \frac{0.8625 - 0.5125}{4\tau - 2\tau}$$

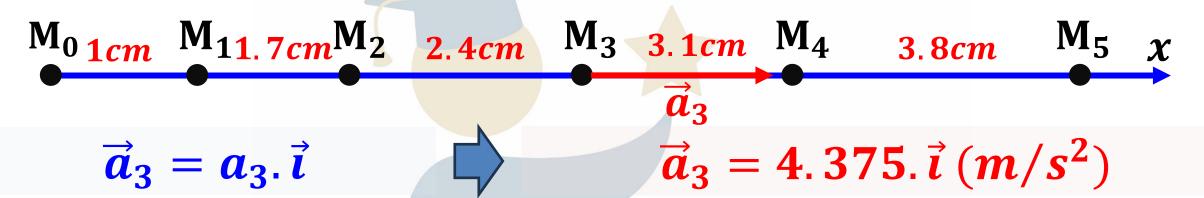
$$a_3 = \frac{0.35}{2 \times \tau}$$



$$a_1 = 4.375 m/s^2$$



3. Determine the characteristics of instantaneous acceleration vector at  $M_3$ .



Origin:  $M_3$ 

Line of action: Horizontal

direction: Right

**magnitude:**  $a_3 = 4.375m / s^2$ 

$$1cm \rightarrow 1.45m/s^2$$

$$x = ?? \rightarrow 4.375 m/s^2$$

$$x = \frac{1cm \times 4.375}{1.45} \approx 3cm$$



## **Important notes**

If the value of a is positive (a>0)

If the value of a is negative (a<0):

The motion called accelerated.

V and a have same sense).

The motion called decelerated.

V and a have opposite sense).

